

# Rickart matrices over commutative rings

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**ABSTRACT.** An element of a unital ring is termed right Rickart if its right annihilator is a principal right ideal generated by an idempotent. This paper investigates the properties of right Rickart elements in general rings, with particular emphasis on their behavior in matrix rings over various classes of commutative rings where idempotents are diagonalizable.

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