

# Semiprime rings with multiplicative(generalized)-derivations involving left multipliers

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**ABSTRACT.** Let  $R$  be a semiprime ring,  $I$  a non zero ideal of  $R$ . A mapping  $F : R \rightarrow R$  (not necessarily additive) is said to be a multiplicative (generalized)-derivation of  $R$  if  $F(xy) = F(x)y + xd(y)$  holds for all  $x, y \in R$ , where  $d$  is any mapping on  $R$ . A map  $H : R \rightarrow R$  (not necessarily additive) is called a multiplicative left multiplier if

$$H(xy) = H(x)y, \text{ holds for all } x, y \in R.$$

The main objective of this article is to study the following situations:

- (i)  $F(xoy) \pm H(xoy) = 0$ ,
  - (ii)  $F(xoy) \pm H[x, y] = 0$ ,
  - (iii)  $F[x, y] \pm [x, H(y)] = 0$ ,
  - (iv)  $F(xoy) \pm [x, H(y)] = 0$ ,
  - (v)  $F(xy) \pm [x, H(y)] \in Z(R)$ ,
  - (vi)  $F(xy) \pm [H(x), H(y)] \in Z(R)$ ,
- for all  $x, y$  in some appropriate subsets of  $R$ .

## 1. INTRODUCTION

Let  $R$  denote an associative ring with center  $Z(R)$ . A ring  $R$  is called a prime ring if for any  $a, b \in R$ ,  $aRb = 0$  implies that either  $a = 0$  or  $b = 0$  and is called a semiprime ring if  $aRa = 0$  implies that  $a = 0$ . For any  $x, y \in R$ , we shall denote the commutator and anti-commutator by the symbols

$$[x, y] = xy - yx$$

and

$$(xoy) = xy + yx,$$

respectively.

An additive map  $d : R \rightarrow R$  is called a derivation of  $R$  if

$$d(xy) = d(x)y + xd(y)$$

holds for all  $x, y \in R$ .

An additive mapping  $F : R \rightarrow R$  associated with a derivation  $d : R \rightarrow R$  is called a generalized derivation of  $R$  if

$$F(xy) = F(x)y + xd(y),$$

holds for all  $x, y \in R$ .

In [6], Bresar introduced the notion of generalized derivation. Obviously, every derivation is a generalized derivation of  $R$ . Thus, generalized derivation covers both the concept of derivation and the concept of left multipliers. Let  $S$  be a non-empty subset of  $R$ .

A map  $f : S \rightarrow R$  is called a centralizing(commuting) map on  $S$  if

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$[f(x), x] \in Z(R)$  ( or  $[f(x), x] = 0$ ), for all  $x \in S$ .

The concept of multiplicative derivations appears for the first time in the work of Daif [9] and it was motivated by the work of Martindale [18]. According to Daif [9]: A map  $d : R \rightarrow R$  is called a multiplicative derivation of  $R$  if  $d(xy) = d(x)y + xd(y)$  holds for all  $x, y \in R$ . Further, the complete description of those maps were given by Goldmann and semrl in [13]. The notion of multiplicative derivation was extended to multiplicative generalized derivation by Daif and Tammam-El-Sayiad [11] as follows: a map  $F : R \rightarrow R$  is called a multiplicative generalized derivation if there exists a derivation  $d$  such that

$$F(xy) = F(x)y + xd(y)$$

for all  $x, y \in R$ .

Recently, Dhara and Ali [12] gave a definition of multiplicative(generalized)-derivation as follows: a mapping  $F : R \rightarrow R$  (not necessarily additive) is said to be multiplicative (generalized)-derivation if

$$F(xy) = F(x)y + xd(y)$$

holds for all  $x, y \in R$ , where  $d$  is any map on  $R$  (not necessarily a derivation nor additive). Hence the concept of multiplicative (generalized)-derivation covers the concept of multiplicative derivation. A mapping  $H : R \rightarrow R$  (not necessarily additive) is said to be a multiplicative left multiplier if

$$H(xy) = H(x)y$$

holds for all  $x, y \in R$  ([19]).

Moreover, multiplicative(generalized)-derivation with  $d = 0$  covers the concept of multiplicative left multipliers. Many papers in literature have investigated the commutativity of prime and semiprime rings satisfying certain functional identities involving multiplicative generalized derivations or multiplicative(generalized)-derivations ([3], [4], [5], [7], [15], [16], [17], [20], [21] and [22]).

Daif and Bell [10] proved that if a semiprime ring  $R$  admits a derivation  $d$  such that  $d[x, y] \pm [x, y] = 0$  holds for all  $x, y$  in a non-zero ideal  $I$  of  $R$ , then  $R$  is commutative. Hongan [14] generalized these results by taking the same situations in the center of the ring  $R$ . Asma Ali et al.[1] investigated the commutativity of a prime ring admitting a generalized derivation satisfying any one of the following identities: (i)  $F([x, y]) \pm [x, y] \in Z(R)$  (ii)  $F(xoy) \pm (xoy) \pm Z(R)$  in some appropriate subset of  $R$ . Recently, Ali et al.[2] proved multiplicative(generalized)-derivation and left ideals in semiprime rings. Dedem Camci and Neset Aydin [8] studied the following identities related to multiplicative(generalized)-derivations in semiprime rings:

- (i)  $F(xy) \pm H(xy) = 0$ ,
- (ii)  $F(xy) \pm H(yx) = 0$ ,
- (iii)  $F(x)F(y) \pm H(xy) = 0$ ,
- (iv)  $F(xy) \pm H(xy) \in Z$ ,
- (v)  $F(xy) \pm H(yx) \in Z$ ,
- (vi)  $F(x)F(y) \pm H(xy) \in Z$ ,

for all  $x, y \in R$ .

In this line of investigation, it is more interesting to study the semiprime rings with multiplicative(generalized)-derivations involving left multipliers in some appropriate subsets of  $R$ .

Throughout the paper,  $R$  will be a semiprime ring,  $I$  a non zero ideal of  $R$ ,  $F$  be a multiplicative(generalized)-derivation of  $R$  and  $H$  be a multiplicative left multiplier of  $R$ .

We shall frequently use the following basic commutator and anti-commutator identities in the proofs of our results:

- (i)  $[x, yz] = y[x, z] + [x, y]z$ ,  
(ii)  $[xy, z] = [x, z]y + x[y, z]$ ,  
(iii)  $xoyz = (xoy)z - y[x, z] = y(xoz) + [x, y]z$ ,  
(iv)  $xyozy = x(yoz) - [x, z]y = (xoz)y + x[y, z]$ ,  
for all  $x, y, z \in R$ .

## 2. MAIN RESULTS

We begin with our first theorem:

**Theorem 2.1.** *Let  $R$  be a semiprime ring and  $I$  a non-zero ideal of  $R$ . If  $F : R \rightarrow R$  is a multiplicative(generalized)-derivation associated with a map  $d : R \rightarrow R$  such that  $F(xoy) \pm H(xoy) = 0$  for all  $x, y \in I$ , then  $I[x, d(x)] = 0$  for all  $x \in I$ .*

*Proof.* By the hypothesis, we have

$$F(xoy) \pm H(xoy) = 0, \text{ for all } x, y \in I. \quad (2.1)$$

Replacing  $y$  by  $yx$  in (2.1), we obtain

$$F((xoy)x) \pm H((xoy)x) = 0,$$

Using (2.1), it reduces to

$$(xoy)d(x) = 0, \text{ for all } x, y \in I. \quad (2.2)$$

Substituting  $d(x)y$  for  $y$  and using (2.2), we get

$$[x, d(x)]yd(x) = 0, \text{ for all } x, y \in I. \quad (2.3)$$

Right multiplying (2.3) by  $x$ , we get

$$[x, d(x)]yd(x)x = 0, \text{ for all } x, y \in I. \quad (2.4)$$

Replace  $y$  by  $yx$  in (2.3), we obtain

$$[x, d(x)]yxd(x) = 0, \text{ for all } x, y \in I. \quad (2.5)$$

subtract (2.4) from (2.5), we get

$$[x, d(x)]y[x, d(x)] = 0, \text{ for all } x, y \in I. \quad (2.6)$$

Replacing  $y$  by  $ry$ , we obtain

$$[x, d(x)]ry[x, d(x)] = 0, \text{ for all } x, y \in I \text{ and } r \in R. \quad (2.7)$$

left multiplying (2.7) by  $y$ , we get

$$y[x, d(x)]Ry[x, d(x)] = 0, \text{ for all } x, y \in I.$$

By the semiprimeness of  $R$ , we conclude that  $y[x, d(x)] = 0$ , for all  $x, y \in I$ ,  
that is,  $I[x, d(x)] = 0$ , for all  $x \in I$ . □

**Theorem 2.2.** *Let  $R$  be a semiprime ring and  $I$  a non-zero ideal of  $R$ . If  $F : R \rightarrow R$  is a multiplicative(generalized)-derivation associated with a map  $d : R \rightarrow R$  such that  $F(xoy) \pm H[x, y] = 0$  for all  $x, y \in I$ , then  $I[x, d(x)] = 0$  for all  $x \in I$ .*

*Proof.* By the hypothesis, we have

$$F(xoy) \pm H[x, y] = 0, \text{ for all } x, y \in I. \quad (2.8)$$

Replacing  $y$  by  $yx$  in (2.8), we obtain

$$F((xoy)x) \pm H([x, y]x), \text{ for all } x, y \in I, \quad (2.9)$$

Using (2.8), it reduces to

$$(xoy) d(x) = 0, \text{ for all } x, y \in I. \quad (2.10)$$

Using the same arguments after (2.2) in the proof of Theorem (2.1), we get the required result.  $\square$

**Theorem 2.3.** *Let  $R$  be a semiprime ring and  $I$  a non-zero ideal of  $R$ . If  $F : R \rightarrow R$  is a multiplicative(generalized)-derivation associated with a map  $d : R \rightarrow R$  such that  $F[x, y] \pm [x, H(y)] = 0$  for all  $x, y \in I$ , then  $I[x, d(x)] = 0$  for all  $x \in I$ .*

*Proof.* By the hypothesis, we have

$$F[x, y] \pm [x, H(y)] = 0 \text{ for all } x, y \in I. \quad (2.11)$$

Replacing  $y$  by  $yx$  in (2.11), we obtain

$$F([x, y]x) \pm [x, H(y)x] = 0 \text{ for all } x, y \in I, \quad (2.12)$$

Using (2.11), it reduces to

$$[x, y] d(x) = 0 \text{ for all } x, y \in I. \quad (2.13)$$

Substituting  $d(x)y$  for  $y$  and using (2.13), we get

$$[x, d(x)] y d(x) = 0 \text{ for all } x, y \in I. \quad (2.14)$$

Right multiplying (2.14) by  $x$ , we obtain

$$[x, d(x)] y d(x) x = 0 \text{ for all } x, y \in I. \quad (2.15)$$

Replacing  $y$  by  $yx$  in (2.14), we get

$$[x, d(x)] y x d(x) = 0 \text{ for all } x, y \in I. \quad (2.16)$$

Subtracting (2.15) from (2.16), we get

$$[x, d(x)] y [x, d(x)] = 0 \text{ for all } x, y \in I. \quad (2.17)$$

Replacing  $y$  by  $ry$ , we obtain

$$[x, d(x)] ry [x, d(x)] = 0 \text{ for all } x, y \in I \text{ and } r \in R. \quad (2.18)$$

left multiplying (2.17) by  $y$ , we get

$$y [x, d(x)] Ry [x, d(x)] = 0 \text{ for all } x, y \in I.$$

The semiprimeness of  $R$  yields that  $y [x, d(x)] = 0$  for all  $x, y \in I$ . Therefore  $I[x, d(x)] = 0$  for all  $x \in I$ .  $\square$

**Theorem 2.4.** *Let  $R$  be a semiprime ring and  $I$  a non-zero ideal of  $R$ . If  $F : R \rightarrow R$  is a multiplicative(generalized)-derivation associated with a map  $d : R \rightarrow R$  such that  $F[x, y] \pm [x, H(y)] = 0$  for all  $x, y \in I$ , then  $I[x, d(x)] = 0$  for all  $x \in I$ .*

*Proof.* By the hypothesis, we have

$$F(xoy) \pm [x, H(y)] = 0 \text{ for all } x, y \in I. \quad (2.19)$$

Replacing  $y$  by  $yx$  in (2.19), we get

$$F((xoy)x) \pm [x, H(y)x] = 0 \text{ for all } x, y \in I, \quad (2.20)$$

Using (2.19), it reduces to

$$(xoy) d(x) = 0 \text{ for all } x, y \in I. \quad (2.21)$$

Then by the same argument as in the proof of Theorem(2.1), we get  $I[x, d(x)] = 0$  for all  $x \in I$ .  $\square$

**Theorem 2.5.** *Let  $R$  be a semiprime ring and  $I$  a non-zero ideal of  $R$ . If  $F : R \rightarrow R$  is a multiplicative(generalized)-derivation associated with a map  $d : R \rightarrow R$  such that  $F(xy) \pm [x, H(y)] \in Z(R)$  for all  $x, y \in I$ , then  $I[d(x), x] = 0$  for all  $x \in I$ .*

*Proof.* By the hypothesis, we have

$$F(xy) + [x, H(y)] \in Z(R) \text{ for all } x, y \in I. \quad (2.22)$$

Replacing  $y$  by  $yz$  in (2.22), we get

$$\begin{aligned} F(xy)z + xyd(z) + H(y)[x, z] + [x, H(y)]z &\in Z(R) \text{ for all } x, y, z \in I, \\ (F(xy) + [x, H(y)])z + xyd(z) + H(y)[x, z] &\in Z(R). \end{aligned} \quad (2.23)$$

Combining (2.21) and (2.22), we obtain

$$[xyd(z), z] + [H(y)[x, z], z] = 0. \quad (2.24)$$

Replacing  $x$  by  $xz$  in (2.23), we get

$$\begin{aligned} [xzyd(z), z] + [H(y)[xz, z], z] &= 0, \\ [xzyd(z), z] + [H(y)[x, z]z, z] &= 0. \end{aligned} \quad (2.25)$$

Right multiplying (2.23) by  $z$  and subtracting from (2.24), we get

$$x[yd(z), z] = 0 \text{ for all } x, y, z \in I. \quad (2.26)$$

Replacing  $x$  by  $wx$  in (2.25) and using (2.25), we obtain

$$[w, z]x[yd(z), z] = 0 \text{ for all } x, y, z, w \in I. \quad (2.27)$$

Replacing  $w$  by  $yd(z)$  and using semiprimeness of  $R$ , we get

$$[yd(z), z] = 0 \text{ for all } y, z \in I. \quad (2.28)$$

Substituting  $d(z)y$  instead of  $y$  in (2.27) and using (2.27), we obtain

$$[d(z), z]yd(z) = 0 \text{ for all } y, z \in I.$$

Replacing  $z$  by  $x$ , we get

$$[d(x), x]yd(x) = 0 \text{ for all } x, y \in I. \quad (2.29)$$

Replacing  $y$  by  $yx$  in (2.28), we get

$$[d(x), x]yxd(x) = 0 \text{ for all } x, y \in I. \quad (2.30)$$

Right multiplying (2.28) by  $x$ , we get

$$[d(x), x]yd(x)x = 0 \text{ for all } x, y \in I. \quad (2.31)$$

Subtracting (2.29) from (2.30), we get

$$[d(x), x]y[d(x), x] = 0 \text{ for all } x, y \in I. \quad (2.32)$$

Replacing  $y$  by  $ry$  in (2.31), we obtain

$$[d(x), x]ry[d(x), x] = 0 \text{ for all } x, y \in I \text{ and } r \in R. \quad (2.33)$$

Left multiplying (2.32) by  $y$ , we get

$$y[d(x), x]Ry[d(x), x] = 0 \text{ for all } x, y \in I. \quad (2.34)$$

By semiprimeness of  $R$ , we conclude that  $y[x, d(x)] = 0$ , for all  $x, y \in I$ , then

$$I[x, d(x)] = 0, \text{ for all } x \in I.$$

In the same manner the conclusion can be obtained when

$$F(xy) - [x, H(y)] \in Z(R) \text{ for all } x, y \in I. \quad \square$$

**Theorem 2.6.** Let  $R$  be a semiprime ring and  $I$  a non-zero ideal of  $R$ . If  $F : R \longrightarrow R$  is a multiplicative(generalized)-derivation associated with a map  $d : R \longrightarrow R$  such that

$$F(xy) \pm [H(x), H(y)] \in Z(R),$$

for all  $x, y \in I$ , then

$$I[d(x), x] = 0,$$

for all  $x \in I$ .

*Proof.* By the hypothesis, we have

$$F(xy) + [H(x), H(y)] \in Z(R), \text{ for all } x, y \in I. \quad (2.35)$$

Replacing  $y$  by  $yz$  in (2.35), we get

$$F(xy)z + xyd(z) + H(y)[x, z] + [H(x), H(y)]z \in Z(R). \quad (2.36)$$

Combining (2.34) and (2.35), we obtain

$$[xyd(z), z] + [H(y)[x, z], z] = 0, \text{ for all } x, y, z \in I. \quad (2.37)$$

Replacing  $x$  by  $xz$  in (2.37), we find that

$$\begin{aligned} [xzyd(z), z] + [H(y)[xz, z], z] &= 0, \\ [xzyd(z), z] + [H(y)[x, z]z, z] &= 0, \text{ for all } x, y, z \in I. \end{aligned} \quad (2.38)$$

Then by the same argument as in the proof of Theorem(2.5), we get  $I[d(x), x] = 0$ , for all  $x \in I$ .

In the same manner the conclusion can be obtained when  $F(xy) - [H(x), H(y)] \in Z(R)$  for all  $x, y \in I$ .  $\square$

**Corollary 2.1.** Let  $R$  be a semiprime ring admitting a multiplicative(generalized)-derivation  $F : R \longrightarrow R$  associated with a map  $d : R \longrightarrow R$  and  $H : R \longrightarrow R$  be a multiplicative left multiplier. If  $R$  satisfies any one of the following identities:

- (i)  $F(xoy) \pm H(xoy) = 0$ ,
- (ii)  $F(xoy) \pm H[x, y] = 0$ ,
- (iii)  $F[x, y] \pm [x, H(y)] = 0$ ,
- (iv)  $F(xoy) \pm [x, H(y)] = 0$ ,
- (v)  $F(xy) \pm [x, H(y)] \in Z(R)$ ,
- (vi)  $F(xy) \pm [H(x), H(y)] \in Z(R)$  holds for all  $x, y \in R$ , then the map  $d$  is a commuting map on  $R$ .

**Example 2.1.** Consider  $R = \left\{ \begin{pmatrix} 0 & a & b \\ 0 & 0 & c \\ 0 & 0 & 0 \end{pmatrix} / a, b, c \in Z \right\}$ , where  $Z$  is set of integers. We

define the maps  $F, d, H : R \longrightarrow R$  by  $F \begin{pmatrix} 0 & a & b \\ 0 & 0 & c \\ 0 & 0 & 0 \end{pmatrix} = \begin{pmatrix} 0 & 0 & b \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}$ ,

$$d \begin{pmatrix} 0 & a & b \\ 0 & 0 & c \\ 0 & 0 & 0 \end{pmatrix} = \begin{pmatrix} 0 & a & b^2 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}, H \begin{pmatrix} 0 & a & b \\ 0 & 0 & c \\ 0 & 0 & 0 \end{pmatrix} = \begin{pmatrix} 0 & 0 & ab \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix},$$

respectively.

It is verified that  $F$  is a multiplicative (generalized)-derivation associated with a map  $d$  respectively and

$$H(xy) = H(x)y$$

holds for all  $x, y \in R$ .

It is easy to see that the identity

$$F(xoy) \pm H(xoy) = 0,$$

for all  $x, y \in R$ .

Here  $R$  is not semiprime because  $\begin{pmatrix} 0 & 1 & 1 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} R \begin{pmatrix} 0 & 1 & 1 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} = (0)$ .

Hence, the condition of semiprimeness in Corollary 2.7 cannot be removed.

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